

Bayesian timing analysis of giant flare of SGR 1806–20 by *RXTE* PCA

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ABSTRACT

Aims. By detecting high frequency quasi-periodic oscillations (QPOs) and estimating frequencies of them during the decaying tail of giant flares from Soft Gamma-ray Repeaters (SGRs) useful constraints for the equation of state (EoS) of superdense matter may be obtained via comparison with theoretical predictions of eigenfrequencies.

Methods. We used the data collected by the Rossi X-Ray Timing Explorer (*RXTE/XTE*) Proportional Counter Array (PCA) of a giant flare of SGR 1806–20 on 2004 Dec 27 and applied a Bayesian periodicity detection method (Gregory & Loredo, 1992) for the search of oscillations of transient nature.

Results. In addition to the already detected frequencies, we found a few new frequencies ($f_{QPOs} \sim 16.9, 21.4, 36.4, 59.0, 116.3$ Hz) of oscillations predicted by Colaiuda et al. (2009) based on the *APR*₁₄ EoS (Akmal et al., 1998) for SGR 1806–20.

Key words. SGR 1806-20 – Soft Gamma-ray Repeaters – Giant flares – QPOs – X-ray timing – Bayesian statistics

1. Introduction

The study of periods of activity of Soft Gamma-ray Repeaters (SGRs, for a recent review see Mereghetti 2008) showing recurrent bursts with sub-second duration and much more extreme events known as giant flares (on rare occasions), may have an important input to our understanding of neutron stars (NSs).

In particular, the detection and analysis of the presence of quasiperiodic oscillations (QPOs), up to a few kHz, has triggered a number of theoretical studies for prediction and direct comparison with various equations of state for superdense matter. These oscillations have been interpreted initially as torsional oscillations of the crust (Samuelsson & Andersson 2007; Sotani et al. 2007). While later the Alfvén oscillations of the fluid core have been taken into account (Levin 2007; Sotani et al. 2008b; Colaiuda et al. 2009; Cerdá-Durán et al. 2009; van Hoven & Levin 2010; Gabler et al. 2010; Colaiuda & Kokkotas 2010). These studies suggested how the observations can constrain both the mass, the radius, the thickness of the crust and the strength of magnetic field of NSs. In particular, the timing analysis of the decaying tail of the unprecedented giant flare of SGR 1806–20 on 2004 Dec 27, allowed to detect QPO frequencies approximately at 18, 26, 30, 92, 150, 625, and 1840 Hz (Israel et al. 2005; Watts & Strohmayer 2006; Strohmayer & Watts 2006; Watts & Strohmayer 2007) in different time intervals, different rotation phase and different amplitudes of oscillations, by means of computation and analysis of the averaged power spectrum.

Here, we present the results of a Bayesian approach of timing analysis, of the giant flare data set of SGR 1806–20 registered on 2004 Dec 27 by *RXTE* PCA, for detecting a periodic signal of unknown shape and period developed by Gregory & Loredo (1992) (for its sensitivity and advantages see further and also Gregory & Loredo 1996).

2. Observational data and results of analysis

The giant flare of SGR 1806–20 has been observed by many space based missions. The data recorded by *RXTE* PCA instrument, consisting of five Xenon-filled detectors covering the energy range 2–50 keV, used the configuration GoodXenon, which records all good events detected in the Xenon chamber with full timing accuracy of 1 μ s. Publicly available data were retrieved by the *XTE* Data Finder (XDF) user interface (Rots & Hilldrup 1997). Event data files have been created and photon arrival times were corrected for the solar barycenter using scripts provided in the package *XTE* *ftools*. The data set consists of 698770 registered photons. However, during the initial intensive spike phase of the giant flare the detectors were saturated. For that reason, in our analysis we use the data after ~ 8.9 sec of the flare onset, consisting of ~ 650000 photon arrival times, clearly covering 51 rotational cycles of SGR 1806–20 (see Fig. 1).

It is clear that observational detection and parameter estimation of QPO frequencies may play a crucial role for testing any theory predicting eigenfrequencies of the neutron star. In this connection, timing analysis of complex flare data set of SGR 1806–20, with the aim of QPO detection, may be divided into several mutually connected, challenging problems. They include the significance of quasi-periodic signal detection and parameter estimation with high precision. Indeed, the decaying tail, of the giant flare of SGR 1806–20, itself has a bumpy structure, very complex light curve shape modulated by rotation of the neutron star (see Fig. 1).

The most widely-used procedure for detection of QPOs is an analysis of the power spectrum calculated from the Fast Fourier transform (FFT) of *uniformly* sampled data. Application of the FFT to unevenly spaced arrival time series data requires binning of the data to produce *equally* spaced samples. Binning is a subjective procedure; the choice of the bin width and edges can affect the apparent significance of a detection and limits sensitiv-

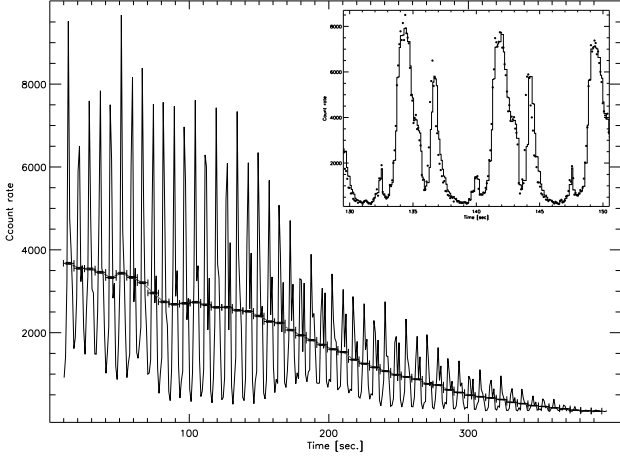


Fig. 1. Light curve of the *RXTE* giant flare of SGR 1806–20 observed on 27th of December 2004. The general decay of the giant flare with a bumpy structure on top of it, namely a strongly periodic signal due to rotation (7.56 sec). The inset panel shows the rotational modulated light curve (filled circles) together with fitted piecewise constant model (solid line, Hutter 2007), shown here only for 2.5 rotational cycles, with a very complex light curve structure (see text for details).

ity on short time scales. Moreover, the presence of the so-called red-noise (low frequency signal in the data, i.e. large calculated power can appear at low frequency because of long-timescale features of the data and at high frequencies from higher harmonics of complex shape strong periodic signal), may cause certain problems with the interpretation of the results (e.g. Bretthorst 1988). In the previous timing analysis of the giant flare data set of SGR 1806–20 by Israel et al. (2005) and Watts & Strohmayer (2006), an averaged power spectrum was considered. Namely, for each rotational cycle or certain rotational phase interval of SGR 1806–20 an independent classical power spectrum was determined depending on the phase of rotation and decaying tail of the giant flare, which were co-added and averaged subsequently. This approach divides the data set into small time intervals, which automatically reduces the significance of any periodicity detection of transient nature and may cause problems related to the windowing of the data sets (van der Klis 1989; Galleani et al. 2001). The complex shape of the light curve (rotational modulation and decaying tail of flare light curves, Fig. 1) is not taken into account in a proper way, i.e. assuming that during small time/phase intervals there are no significant intrinsic variations in the data subsets. Moreover, in some circumstances FFT may fail to detect the periodic signal (see e.g. Bretthorst 1988; Gregory & Loredo 1996). As explicitly shown by Jaynes (1987) (see also, Bretthorst 1988, 2001; Gregory 2005) the probability for the frequency of a periodic sinusoidal signal is given approximately by

$$p(f_n|D, I) \propto \exp \left[\frac{C(f_n)}{\sigma^2} \right], \quad (1)$$

where $C(f_n)$ is the squared magnitude of the FFT, showing that proper approach to convert $C(f_n)$ into probabilities involves first dividing by the noise variance and then exponentiating, which suppresses spurious ripples in the power spectrum.

We used a procedure which does not require binning and takes into consideration the rotational modulation and decaying

tail of the flare (Bretthorst 1988; Gregory & Loredo 1992, 1996; Jaynes & Bretthorst 2003; Vaughan 2009).

For the analysis of the data for the search of QPOs during the giant flare of SGR 1806–20, we applied a Bayesian method developed by Gregory & Loredo (1992) (hereafter referred to as the GL method) for the search of pulsed emission from pulsars in X-ray data, consisting of the arrival times of events, when we have no specific prior information about the shape of the signal. As a particular case of QPO can be considered a periodic signal with some length of coherence ($Q \equiv \nu_0/2\sigma$, ν_0 is the centroid of the frequency and σ half width at half maximum), i.e. a periodic signal with additional parameters of the oscillation with start and end times¹.

The GL method for timing analysis first tests if a constant, variable or periodic signal is present in a data set.

In the GL method, periodic models are represented by a signal folded into trial frequency with a light curve shape as a stepwise function with m phase bins per period plus a noise contribution. With such a model we are able to approximate a phase folded light curve of any shape. Hypotheses for detecting periodic signals represents a class of stepwise periodic models with the following parameters: trial period, phase, noise parameter and number of bins (m). The most probable model parameters are then estimated by marginalization of the posterior probability over the prior specified range of each parameter. In Bayesian statistics posterior probability contains a term that penalizes complex models (unless there is no significant evidence to support that hypothesis), hence we calculate the posterior probability by marginalizing over a range of models, corresponding to a prior range of number of phase bins, m , from 2 to 12. Moreover, the GL method is well suited for variability detection, i.e. to characterize an arbitrary shape light curve with piecewise constant function $Z(t)$ (Rots 2006).

For the search and detection of QPOs we used a slightly different version of the GL method: First we determine $Z(t)$ - fitting with a piecewise constant model (solid line in the inset panel of the Fig. 1, Hutter 2007)

to characterize the complex light curve shape in the data set, giant flare decaying tail and rotational modulated light curve. Then we subsequently compare competing hypothesis, i.e. whether the data support a purely piecewise constant or piecewise constant+periodic model. If there is an indication of the presence of a periodic signal (e.g. odds ratio of competing models exceeding 1, see also Gregory & Loredo (1992, 1996))

we determine also the time intervals where it has its maximum strength (e.g. amplitude or pulsed fraction) via a Markov Chain Monte Carlo (MCMC) approach using QPO start and end times as free parameters.

Finally, in the latter case, we estimate parameters (frequency, phase, amplitude, coherence length of QPO, etc.) of the periodic signal with high precision. For example, in order to estimate the frequency of a periodic signal the posterior probabilities density function used:

$$p(\omega|D, M_m) = \frac{C}{\omega} \int_0^{2\pi} d\phi \frac{1}{W_m(\omega, \phi)}, \quad (2)$$

where $C = \left[\int_{\omega_{lo}}^{\omega_{hi}} \frac{d\omega}{\omega} \int_0^{2\pi} d\phi \frac{1}{W_m(\omega, \phi)} \right]^{-1}$ and $W_m(\omega, \phi) = \frac{N!}{n_1!n_2!\dots n_m!}$ is the number of ways the binned distribution could have arisen "by chance", $n_j(\omega, \phi)$ is the number of events falling into the j th of m phase bins given the frequency, ω , and phase, ϕ , and N is

¹ More strictly: coherent transient signal (van der Klis 2010)

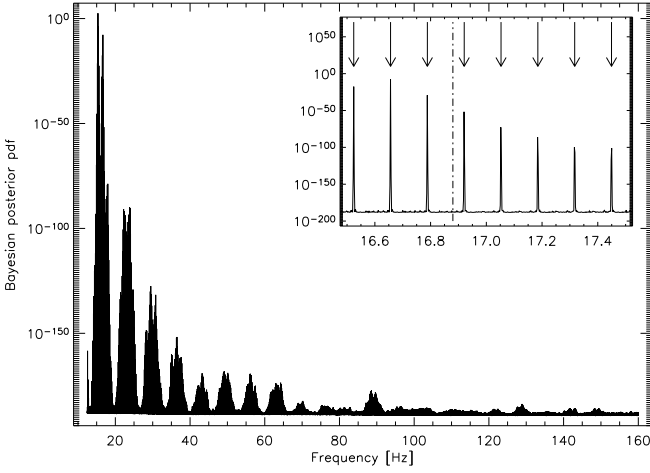


Fig. 2. Application of the GL method for blind periodicity search to the complete data set obtained by *RXTE PCA* of giant flare of SGR 1806–20 2004 Dec 27 revealed a strong coherent signal at the frequency of 0.13219244 Hz and higher harmonics up to 100Hz. Bayesian posterior probability density vs frequencies in the range of 12.0–160 Hz is shown. The inset panel shows a zoomed part of it around 16.88 Hz. Arrows are indicating higher harmonics (from 125 to 132) of the fundamental frequency and the dash-dotted vertical line shows one of the detected QPO frequency in a short time interval (see text, for details).

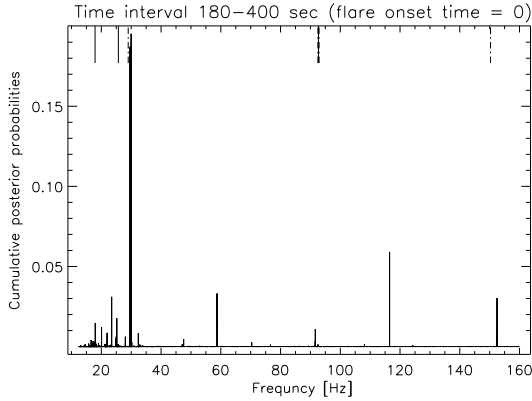


Fig. 3. The Bayesian posterior probability density vs. trial frequency of the periodic signal for the giant flare data set of SGR 1806–20. QPO frequencies already detected by averaged power spectrum analysis and also with other mission *RHESSI* (Israel et al. 2005; Watts & Strohmayer 2006) are marked as small lines at the top axis. Those QPO frequencies are also detected by us. In addition, we have detected several more QPO frequencies (21, 59 and 116 Hz) with the Bayesian method, which were also predicted by Colaiuda et al. (2009).

the total number of photons (for details, see Gregory & Loredó 1992).

First, we applied the GL method as implemented by Gregory & Loredó (1992) to the 2004 Dec 27 giant flare whole data set of SGR 1806–20 observed by *RXTE PCA* and started the timing analysis by performing a blind periodicity search in the range of 12.0–160 Hz. Naturally, we found a very strong coherent signal at ~ 7.56 s, the pulsation period of the NS, followed by higher harmonics up to the 100Hz (see Fig. 2).

Next, we divided the data set into 51 rotational cycles (see Fig.1). Each of these subsamples were treated as independent

data sets. We determined the Bayesian probability densities versus trial frequency. Final probabilities were derived in two ways; First, as the multiplication (the likelihood) of those independent Bayesian posterior probability density functions; and the second one simply summing those independent probabilities² (see Fig.3).

This approach also revealed a number of rotational cycles within which the probability of the model of periodic signal is significantly higher than the constant one. Namely, during time intervals of 183.8–191.2, 244.3–251.9 and 259.4–267.1 seconds, from the flare onset, odds ratios of periodic vs piecewise constant models are ~ 10 , ~ 30 and ~ 197 , correspondingly.

In order to detect start and end times oscillations we included also observational data of neighboring rotational cycles (where an oscillation with that frequency was not detected) and performed the periodicity search for an expanded time interval with additional two free parameters with the MCMC approach with Metropolis-Hastings algorithm. As initial values of these ($t_{QPOstart}$ and t_{QPOend}) parameters served start and end times of an observation, satisfying the condition: $t_{Obs.start} \leq t_{QPOstart} < t_{QPOend} \leq t_{Obs.end}$. Starting with the abovementioned initial values can be considered as a good strategy, since the detected signal has a higher significance in a subinterval of the considered time interval and the fast convergence of the MCMC procedure already provided. This analysis via MCMC revealed even shorter time intervals within which periodic signal is stronger. The estimates of oscillations frequencies and the corresponding 68% interval of the highest probability densities are presented in the Table 1 (see, also Fig. 4,7).

As shown by our intensive simulations, this approach readily detects time intervals where periodic signal has highest and lowest³ strength. Nevertheless, we performed also time-frequency analysis (see Fig. 5 and 6, as well as dynamic power spectrum, van der Klis 1989) and candidate QPOs fitted to a Lorentzian function. We estimated frequency centroids and full widths at half maximums. For significant detections they are presented in Table 1. The coherence values $Q \equiv \nu_0/2\sigma \sim 60$ –200 are indicating on the transient nature of almost perfect periodic signals.

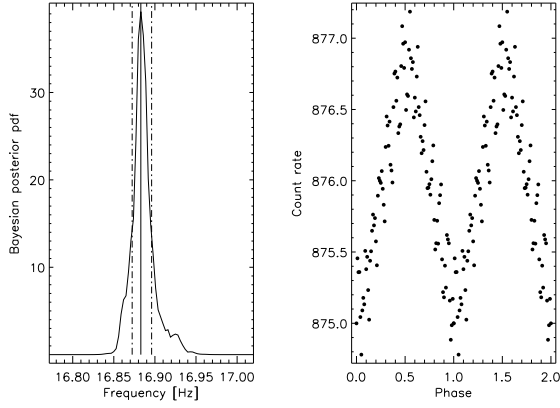
For those significant detections we have also fitted folded light curves with a template function, $\psi(t) = \sum_{i=1}^n A_i \sin[i\omega_0(t - \psi_i)]$, truncating the series at the highest harmonic that was statistically significant after performing an F-test (see Dall’Osso et al. 2003, for details). It turned out that oscillations at 16.9Hz and 36.8 Hz adding the second harmonic does not improve the fit of phase folded light curve (significance levels, accordingly are 0.71 and 0.16), while in the case of 21.3Hz it significantly improves it (significance level of 0.0006. Thus, oscillations at the frequencies of 16.9Hz and 36.8Hz can be considered of sinusoidal shape, and at 21.3Hz not. We obtained similar results by analysing also power spectra, i.e. fitting spectral profiles of them with *sinc* function.

² Addition rule of probabilities: probability that the QPOs at the given frequency are present Δt_1 or Δt_2 or both time intervals, while likelihood (i.e. summed power spectrum) defines the probability of presence QPOs during Δt_1 and Δt_2 (i.e. multiplication rule of probabilities, see also, Eq. 1)

³ A time interval where odds ratio of the models of a periodic and piecewise constant models just exceeds a theoretical minimum, Odds ratio = 1, i.e. both models have equal probability to be true.

Table 1. Detected QPO frequencies not reported in the literature (Israel et al. 2005; Watts & Strohmayer 2006; Strohmayer & Watts 2006).

f_{QPO} [Hz] (68% credible region)	Time intervals of QPOs ^a	Lorentzian centroids(Hz)	$FWHM$ [H]
16.88 ^b (16.87 – 16.90)	259.4–267.1	16.90±0.004	0.12
21.36 ^b (21.35 – 21.38)	244.3–251.9	21.34±0.003	0.35
36.84 ^b (36.83 – 36.88)	183.8–191.2	36.88±0.004	0.24
59.04 (58.58 – 59.28)	146.0–176.2	—	—
61.26 (61.25 – 61.27)	251.9–395.6	—	—
116.27 (116.24 – 116.28)	168.7–198.9	—	—

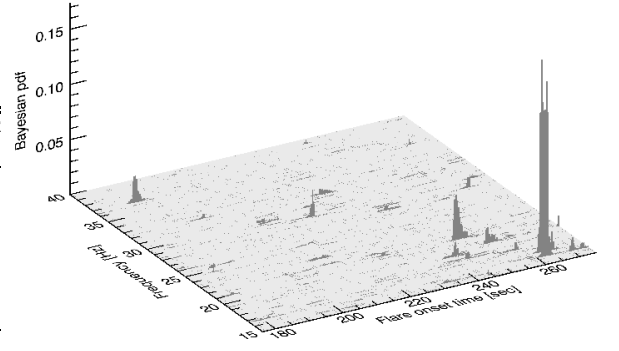
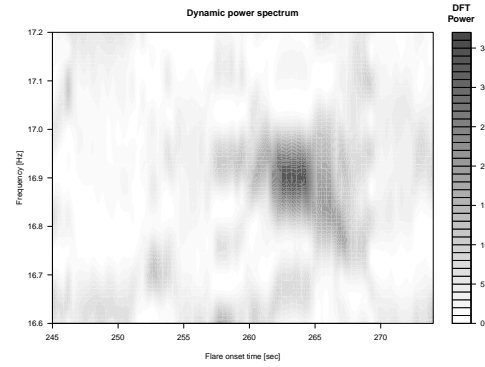
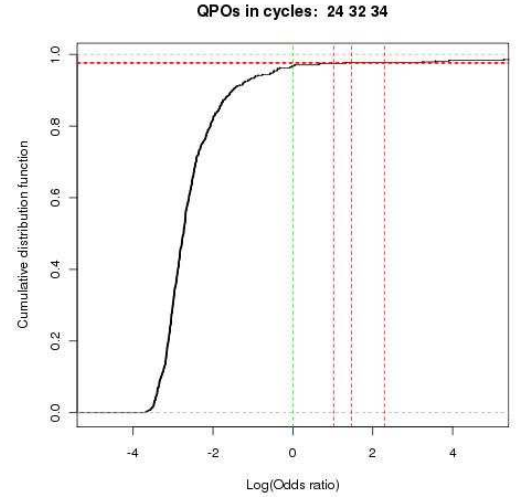
^a Giant Flare onset time is set to 0^b Highly significant detection (for details, see text)**Fig. 4.** Bayesian posterior probability density vs frequencies in the time interval of 259–267 sec from the giant flare onset. By dashed vertical lines are indicated the 68% region of the highest probability density. Odds-ratio of periodic vs constant model is ~ 200 . The right panel depicts the phase folded light curve with frequency $f_{QPO} = 16.88$ Hz, it has almost perfect sinusoidal shape (for details, see text).

3. Discussion

We report the detection of oscillations of transient nature from SGR 1806–20 giant flare decaying tail recorded by the *RXTE* PCA by applying the GL method for periodicity search. We have confirmed the detections of QPOs at frequencies (in the range of 12 – 160 Hz) reported by Watts & Strohmayer (2006) and, in addition, we found some more QPOs at $f_{QPOs} = 16.9, 21.4, 36.8$ Hz with corresponding odds ratios $\sim 197, \sim 30$ and ~ 10 , in shorter time scales, i.e. within individual rotational cycles (see, Fig. 7).

These odds ratios, describing the significance of presence of a periodic signal, are sensitive to the frequency search range. In contrast, detected frequencies of QPOs, found by locating maximums in the posterior probability density function, are insensitive to the prior search range of frequencies. We computed the uncertainty of f_{QPOs} at 68% confidence level by using this posterior probability density function. In addition to that, we have also estimated the significance of our QPO detection by an empirically determined cumulative distribution (see, Fig. 7).

The great variety of neutron star oscillation modes (McDermott et al. 1985) is associated with their global structure as well as their internal characteristics. Neutron star seismology has already been proposed as a tool to understand their internal structure (Kokkotas et al. 2001). The various types of

**Fig. 5.** Bayesian posterior probability density vs frequencies and the time of the giant flare onset. Clearly seen significant detections of oscillations at 16.9, 21.4 and 36.4 Hz. Large $Q \equiv \nu_0/2\sigma$ values (see, Table 1) indicating on the coherent nature of transient oscillations (for details, see text).**Fig. 6.** Dynamic power spectrum of giant flare of SGR1806-20 in the frequency range of 16.5–17.5 Hz and in the time interval of 250–275 sec (see, Table 1).**Fig. 7.** Empirical cumulative distribution function as a function of Odds ratio, i.e. the probability of periodic model vs constant one, on the base of simulations of QPO frequencies with different amplitudes and noise, as much as possible to the observed values in terms of number of registered photons, spanned times, etc.. Detected QPO frequencies indicated by vertical dashed lines, showing a high significance of detections.

oscillations carry information about the equation of state, the thickness of the crust, the mass, radius and even the rotation rate (Gaertig & Kokkotas 2010). Still, modeling a truly realistic oscillating neutron star is difficult, however the potential reward is considerable. This has been demonstrated from the recent theoretical results for the QPOs which have been interpreted as magnetoelastic oscillations. These calculations have shown how the observations constrain both the mass, the radius, the thickness of the crust and the strength of magnetic field of these stars (Sotani et al. 2007; Samuelsson & Andersson 2007; Colaiuda et al. 2009; Cerdá-Durán et al. 2009). While one could even set severe constraints in the geometry of the interior magnetic field (see Sotani et al. 2008a).

In particular, by studying Alfvén oscillations, in the stellar interior, in the absence of crust, Colaiuda et al. (2009) could reveal the existence of Alfvén continua (as suggested by Levin 2007). The edges of this continuum have been used to explain the observed QPOs. It is worth noticing, that QPO frequencies found in this work have been predicted by Colaiuda et al. (2009). More recent calculations by Colaiuda & Kokkotas (2010) taking into account the presence of crust, i.e. the coupled crust-core oscillations, verified the presence of the continuum but in addition they revealed the presence of discrete Alfvén oscillations as well as some extra discrete modes which can be associated with the oscillations of the crust. These new results explain the previous published QPO frequencies but also the ones presented here and set quite severe constraints in the parameters of the neutron star.

4. Conclusions

1. We found new **oscillations of transient nature** applying Bayesian timing analysis method of the decaying tail of the giant flare of SGR 1806–20 2004 Dec 27, observed by *RXTE PCA*, not yet reported in the literature.
2. Some of those **oscillations** frequencies ($f_{QPOs} \sim 17, 22, 37, 56, 112 \text{ Hz}$) are predicted by the theoretical study of torsional Alfvén oscillations of magnetars (see, Table 2, by Colaiuda et al. 2009), suggesting APR_{14} (Akmal et al. 1998) EoS⁴ of SGR 1806–20.
3. These preliminary results are very promising and we plan to extend our high frequency oscillations research (both the theoretical predictions as well as the observations) to both activity periods, as well as to the quiescent state of SGRs and AXPs, as well as to the isolated neutron stars with comparatively smaller magnetic fields.

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⁴ Neutron star models based on the models for the nucleon-nucleon interaction with the inclusion of a parameterized three-body force and relativistic boost corrections, estimating maximum mass and stiffness (see, also Heiselberg & Hjorth-Jensen 1999).